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ANNOTATED COMPUTER OUTPUT

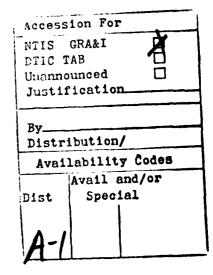
87 - 5

ANNOTATED COMPUTER OUTPUT FOR SPLIT PLOT DESIGN: BMDP 2V

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ANNOTATED COMPUTER OUPUT FOR SPLIT PLOT DESIGN: BMDP 2V

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ABSTRACT

In order to provide an understanding of covariance analyses for split plot designs, analyses are first conducted on a data set without the covariate. Then an analysis with the covariate is performed. The third example has a different experiment design for the whole plots and the covariate is constant for all split plots within a whole plot. Computer packages may only give portions of the analysis correctly. Some packages require two procedural calls to obtain a portion of the correct results. BMDP 2V falls in the above category.

INTRODUCTION

This is part of a continuing project that produces annotated computer output for the analysis of balanced split plot experiments with covariates. The complete project will involve processing three examples on SAS/GLM, BMDP/2V, SPSS-X/MANOVA, GENSTAT/ANOVA, and SYSTAT/MGLH. Only univariate results are considered. We show here the results from BMDP 2V.

For Example 1, the data are artificial and were constructed for ease of computation; the experiment design for the whole plots is a randomized complete block and the split plot treatments are randomly allocated to the split plot experimental units within each whole plot. Example 2 is the same as Example 1 except that a

covariate varies from split plot to split plot. The data for Example 3 come from an experiment wherein the whole plot treatments were laid out in a completely randomized design and the split plot treatments were randomly allotted to the split plot experimental units within each whole plot. The value of the covariate varies from whole plot to whole plot but is constant for all split plots within a whole plot treatment.

We present the elementary computational steps. Simple hypothetical data are used for the first two examples so that it is easy to provide all detailed computations to illustrate how each number is obtained. Some readers may wish to skip the detailed computations. The third example comes from Winer (1971). The detailed computations are given in his book (p. 803).

Data SP-1

Split plot data with whole plots arranged in randomized complete block design (hypothetical data)

				Whol	e plot t	reatmer	nt			
		Wl					W2			
	split	plot	trea	tment		split	plot	trea	tment	
Block	s ₁	s ₂	s ₃	s ₄	Total	s	s ₂	s ₃	s ₄	Total
1	3	4	7	6	20	3	2	1	14	20
2	6	10	1	11	28	8	8	2	18	36
3	6	10_	4	4	24	10	8	9	13	40
Total	15	24	12	21	72	21	18	12	45	96

Total and Means

	Blocks (8 observations)		W(whole plots) (12 observations)			S(split plot) (6 observations)			
	Total	Mean		Total	Mean		Total	<u>Mean</u>	
1	40	5	Wl	72	6	s ₁	36	6	
2	64	8	W2	96	8	s_2^-	42	7	
3	64	8				รู	24	4	
Gran	nd Total	168				s₄	66	11	
Gran	nd Mean	7	_						

Model:
$$Y_{ijk} = \mu + \rho_j + \tau_i + \delta_{ij} + \alpha_k + (\alpha \tau)_{ik} + \epsilon_{ijk}$$
 $\mu = \text{mean}$
 $\tau_i = \text{effect of whole plot i}$
 $\rho_j = \text{effect of block j}$
 $\alpha_k = \text{effect of split plot k}$
 $\delta_{ij} = \text{error (a) effect}$
 $(\alpha \tau)_{ik} = \text{effect of interaction of whole plot i and split plot k}$
 $\epsilon_{ijk} = \text{error (b) effect}$
whole plot i and split plot k

Analysis of Variance

Source	(*)	df	SS
B (Blocks)	$= R(\rho \mu, \tau, \alpha, \alpha \tau)$	2	48
W (whole plot treatments)	$= R(\tau \mu, \rho, \alpha, \alpha \tau)$	1	24
BxW (error (a))	$= R(\delta \mu, \rho, \tau, \alpha, \alpha \tau)$	2	16
S (split plot treatments)	$= R(\alpha \mu, \rho, \tau, \alpha \tau)$	3	156
S×W (interaction of S and W)	$= R(\alpha \tau \mu, \alpha, \tau, \rho)$	3	84
(**) SxB:W (error (b))	$= R(\in [\mu,\alpha,\tau,\alpha\tau,\rho)$	12	112
Total (Corrected for mean)	$= R(\rho, \tau, \delta, \alpha, \alpha\tau, \in \mu)$	23	440
Mean	$= R(\mu)$	1	1176
Total (Uncorrected for mean)	** *	24	1616

(*)Notation follows that of Searle(1971). Since the design is balanced, $R(\rho | \mu, \tau, \alpha, \alpha \tau) = R(\rho | \mu)$, etc. The simpler notation is used later. (**) S×B:W means S×B within W.

Calculations of sums of squares:

$$N = 2 \cdot 3 \cdot 4 = 24 , \quad \overline{Y} = 7$$

$$R(\mu, \rho, \tau, \delta, \alpha, \alpha \tau, \epsilon) = \sum_{i=1}^{2} \sum_{j=1}^{3} \sum_{k=1}^{4} Y_{ijk}^{2} = (3^{2} + 6^{2} + 6^{2} + \cdots + 18^{2} + 13^{2}) = 1616$$

$$R(\mu) = N\tilde{Y}^2 = 24 \cdot (7)^2 = 1176$$

$$R(\rho,\tau,\delta,\alpha,\alpha\tau,\epsilon|\mu) = 1616 - 1176 = 440$$

$$R(\rho | \mu) = R(\mu, \rho) - R(\mu) = \frac{(40^2 + 64^2 + 64^2)}{8} - 1176 = 1224 - 1176 = 48$$

$$R(\tau | \mu) = R(\mu, \tau) - R(\mu) = \frac{(72^2 + 96^2)}{12} - 1176 = 1200 - 1176 = 24$$

$$R(\delta | \mu, \rho, \tau) = R(\delta, \mu, \rho, \tau) - R(\mu, \rho) - R(\tau, \mu) + R(\mu)$$

$$= \frac{(20^2 + 28^2 + 24^2 + 20^2 + 36^2 + 40^2)}{4} - 1224 - 1200 + 1176$$

$$= 1264 - 1224 - 1200 + 1176 = 16$$

$$R(\alpha | \mu) = R(\alpha, \mu) - R(\mu) = \frac{(36^2 + 42^2 + 24^2 + 66^2)}{6} - 1176 = 1332 - 1176 = 156$$

$$R(\alpha \tau | \mu, \alpha, \tau) = R(\alpha \tau, \mu, \alpha, \tau) - R(\mu, \alpha) - R(\mu, \tau) + R(\mu)$$

$$= \frac{(15^2 + 24^2 + 12^2 + 21^2 + 21^2 + 18^2 + 12^2 + 45^2)}{3} - 1332 - 1200 + 1176$$

$$= 1440 - 1332 - 1200 + 1176 = 84$$

$$R(\epsilon | \mu, \rho, \delta, \alpha, \tau, \alpha \tau) = R(\epsilon, \mu, \alpha, \rho, \delta, \tau, \alpha \tau) - R(\mu, \rho, \tau, \delta) - R(\mu, \alpha, \tau, \alpha \tau) + R(\tau, \mu)$$

$$= 1616 - 1264 - 1440 + 1200 = 112$$

Data SP-2

Data SP-2: Data SP-1 with the following covariate Z which varies with split plot

Covariate (Z)

1	whole plot									
			W	1				W	2	
	_s ₁	s ₂	s ₃	S ₄	Total	s ₁	s ₂	s ₃	S ₄	Total
В ₁	1	2	1	2	6	2	0	2	4	8
B ₂	2	2	0	4	8	4	1	3	4	12
B ₃	3	5	2	0	10	3	2	4	7	16
Total	6	9	3	6	24	9	3	9	15	36

Totals and Means

	blocks (8 observations)			W (whole 12 obser		S (split plot) (6 observations)		
	Total	Mean		Total	Mean		Total	Mean
1	14	14/8	1	24	2.0	1	15	2.5
2	20	20/8	2	36	3.0	2	12	2.0
3	26	26/8				3	12	2.0
Gra	nd	·				4	21	3.5
Tot	al 60	2.5						

Model:
$$Y_{ijk} = \mu + \rho_j + \tau_i + \delta_{ij} + \alpha_k + (\alpha \tau)_{ik} + \beta_1 (\bar{z}_{ij} - \bar{z}_{...}) + \beta_2 (z_{ijk} - \bar{z}_{ij}) + \epsilon_{ijk}$$
 $\rho_j = \text{effect of jth block} \qquad \tau_i = \text{effect of ith whole plot}$
 $\alpha_k = \text{effect of kth split plot} \qquad \beta_1 = \text{whole plot regression slope}$
 $\beta_2 = \text{split plot regression slope} \qquad \delta_{ij} = \text{error a} \qquad \epsilon_{ijk} = \text{error b}$

Table of sum of squares and products

Source	df	YY	YZ	ZZ
В	2	48	18	9
W	1	24	12	6
B×W (error a)	2	16	4	1
S	3	156	33	9
S×W	3	84	33	21
SxB:W (error b)	12	112	17	20
Mean	1	1176	420	150
Total	24	1616	537	216

YY column is the same as in SP-1, ZZ column is computed in the same fashion. Thus, only computations for YZ column are illustrated.

$$Total_{YZ} = \sum_{i=1}^{2} \sum_{j=1}^{3} \sum_{k=1}^{4} Y_{ijk} \cdot Z_{ijk}$$

$$= 3(1) + 6(2) + \cdots + 14(4) + 18(4) + 13(7) = 537$$

$$Mean_{YZ} = N\overline{Y} \cdot ... \overline{Z} \cdot ... = \frac{168 \cdot 60}{24} = 420$$

$$B_{YZ} = \frac{\sum_{j=1}^{3} \sum_{i=1}^{2} \sum_{k=1}^{4} Y_{ijk}}{2 \cdot 4} \cdot (\sum_{i=1}^{2} \sum_{k=1}^{2} Z_{ijk}) -420 = \frac{40(14) + 64(20) + 64(26)}{8} - 420$$

$$= 438 - 420 = 18$$

$$W_{YZ} = \frac{\sum_{j=1}^{2} \sum_{j=1}^{3} \sum_{k=1}^{4} Y_{ijk}}{3(4)} \cdot (\sum_{j=1}^{3} \sum_{k=1}^{2} Z_{ijk}) - 420 = 432 - 420 = 12$$

$$B \times W_{YZ} = \frac{\sum_{i=1}^{2} \sum_{j=1}^{3} (\sum_{k=1}^{4} Y_{ijk}) (\sum_{k=1}^{4} Z_{ijk})}{4} - 438 - 432 + 420$$

$$= 454 - 438 - 432 + 420 = 4$$

$$S_{YZ}: \sum_{k=1}^{4} \frac{(\sum_{j=1}^{2} \sum_{j=1}^{3} Y_{ijk}) (\sum_{j=1}^{2} \sum_{j=1}^{3} Z_{ijk})}{2(3)} - 420 = 453 - 420 = 33$$

$$S \times W_{YZ}: \frac{\sum_{j=1}^{2} \sum_{k=1}^{4} (\sum_{j=1}^{3} Y_{ijk}) (\sum_{j=1}^{2} \sum_{j=1}^{3} Z_{ijk})}{3} - 453 - 432 + 420$$

$$= 498 - 453 - 432 + 420 = 33$$

$$S \times B: W_{YZ}: \frac{2}{3} = 4$$

$$\sum_{j=1}^{2} \sum_{k=1}^{3} (\sum_{j=1}^{4} Y_{ijk}) (\sum_{j=1}^{3} Z_{ijk}) - 454 - 498 + 432$$

$$= 537 - 454 - 498 + 432 = 17$$

Analysis of Variance and Covariance

Source		df	SS
B (block)	$= R(\rho \mu, \tau)$	2	48
W (whole plot treatment)	$= R(\rho \mu, \tau)$ $= R(\tau \mu, \rho, \beta_1)$	1	3.4286
Regression (a)	$= R(\beta_1 \mu, \rho, \tau)$	1	16.0
BxW (error (a))	$= R(\delta \mu, \rho, \tau, \beta_1)$	1	0.0
S (split plot treatment)	$= R(\alpha \mu, \rho, \tau, \alpha \tau, \beta_2)$	3	84.243
S×W (interaction of S and W)	$= R(\alpha \tau \mu, \rho, \tau, \alpha, \beta_2)$	3	37.474
Regression (b)	$= R(\beta_2 \mu, \rho, \tau, \alpha, \alpha \tau)$	1	14.450
S×B: W (error (b))	$= R(\epsilon \mu, \rho, \alpha, \tau, \alpha \tau, \beta_2)$	11	97.550

$$\hat{\beta}_1 = B \times W_{YZ} / B \times W_{ZZ} = 4/1 = 4$$

$$\hat{\beta}_2 = S \times B : W_{YZ} / S \times B : W_{ZZ} = 17/20 = 0.85$$

The SS's adjusted by regression on Z are illustrated below:

 $R(\rho | \mu) = 48$, remains same since it is not of interest to adjust for Z on the blocks.

$$R(\tau, \delta | \mu, \rho, \beta_1) = (W_{YY}^+ B \times W_{YY}^-) - \frac{(W_{YZ}^+ B \times W_{YZ}^-)^2}{W_{ZZ}^+ B \times W_{ZZ}^-}$$

$$= (24 + 16) - \frac{(12 + 4)^2}{6 + 1} = 40 - \frac{256}{7} = 3.4286$$

$$R(\delta | \mu, \rho, \tau, \beta_1) = B \times W_{YY} - \frac{(B \times W_{YZ})^2}{B \times W_{ZZ}} = 16 - \frac{4^2}{1} = 0$$

$$R(\tau | \mu, \rho, \beta_1) = R(\tau, \delta | \mu, \rho, \beta_1) - R(\delta | \mu, \rho, \tau, \beta_1)$$
$$= 40 - \frac{256}{7} - 0 = 3.4286$$

$$R(\beta_1 | \mu, \tau, \rho) = \frac{(B \times W_{YZ})^2}{B \times W_{ZZ}} = \frac{4^2}{1} = 16$$

$$R(\alpha, \epsilon | \mu, \rho, \tau, \alpha \tau, \beta_{2}) = (S_{YY} + S \times B : W_{YY}) - \frac{(S_{YZ} + S \times B : W_{YZ})^{2}}{S_{ZZ} + S \times B : W_{ZZ}}$$

$$= (156 + 112) - \frac{(33+17)^{2}}{9+20}$$

$$= 268 - 86.207 = 181.793$$

$$R(\alpha\tau, \epsilon | \mu, \rho, \alpha, \tau, \beta_2) = (S \times W_{YY} + S \times B : W_{YY}) - \frac{(S \times W_{YZ} + S \times B : W_{YZ})^2}{S \times W_{ZZ} + S \times B : W_{ZZ}}$$

$$= 84 + 112 - \frac{(33+17)^2}{21+20} = 196 - 60.976 = 135.024$$

Note: $R(\alpha, \epsilon | \mu, \beta_2)$ and $R(\alpha \tau, \epsilon | \mu, \alpha, \tau, \beta_2)$ are intermediate steps for later use.

$$R(\beta_2 | \mu, \rho, \alpha, \tau, \alpha \tau) = \frac{(S \times B : W_{YZ})^2}{S \times B : W_{ZZ}} = \frac{17^2}{20} = 14.450$$

$$R(\epsilon | \mu, \rho, \alpha, \tau, \alpha \tau, \beta_2) = S \times B : W_{YY} - \frac{(S \times B : W_{YZ})^2}{S \times B : W_{ZZ}} = 112 - \frac{17^2}{20} = 112 - 14.45 = 97.55$$

$$R(\alpha | \mu, \rho, \tau, \alpha \tau, \beta_2) = R(\alpha, \epsilon | \mu, \rho, \tau, \alpha \tau, \beta_2) - SS \text{ error } b = 181.793 - 97.55$$

= 84.243

$$R(\alpha \tau | \mu, \rho, \alpha, \tau, \beta_2) = R(\alpha \tau, \epsilon | \mu, \rho, \alpha, \tau, \beta_2) - R(\epsilon | \mu, \rho, \alpha, \tau, \alpha \tau, \beta_2)$$

$$= 135.024 - 97.55 = 37.474$$

Data SP-3

Split plot data with plots arranged in a completely randomized design and a covariate Z that is constant within the whole plot. (Winer, 1971, p. 803)

whole plot	Subject	Split B ₁	plots B ₂	z	Total	
	<u></u>	Y	Y		Y	
A ₁			 -			
-	1	10	8	3	18	
	2	15	12	5	27	
	3	20	14	8	34	
	44	12	6	2	18	
A ₂						
	5	15	10	1	25	
	6	25	20	8	45	
	7	20	15	10	35	
	8	15	10	2	25	
	Total	132	95	39	227	
	Mean	16.5	11.9	4.88		

Model:
$$y_{ijk} = \mu + \tau_i + \delta_{ij} + \alpha_k + (\tau \alpha)_{ik} + \beta_1(z_{ij} - \overline{z}_{..}) + \epsilon_{ijk}$$

$$\tau_{i}$$
 = A effect (whole plot) δ_{ij} = error (a) ϵ_{ijk} = error (b) α_{k} = B effect (split plot) β_{1} = whole plot regression slope

Analysis of variance and covariance

Source		df	SS
A (whole plot)	$= R(\tau \mu, \beta_1)$	1	44.492
Regression	$= R(\beta_1 \mu, \tau)$	1	166.577
Error (a)	$= R(\delta \mu, \tau, \beta_1)$	5	61.298
B (split plot)	$= R(\alpha \mu, \tau, \alpha \tau)$ $= R(\tau \alpha \mu, \tau, \alpha)$	1	85.563
AxB (interaction)	$= R(\tau \alpha \mu, \tau, \alpha)$	1	0.563
Error (b)	$= R(\epsilon \mu, \tau, \alpha, \tau \alpha)$	6	6.375

Table of SS and products

Symbol	y ²	ZY	z ²
W	68.06	12.38	2.25
E(a)	227.88	163.00	159.50
S	85.563	0	0
WS	0.563	0	0
E(b)	6.375	0	0

$$\hat{\beta}_1 = \frac{163.00}{159.50} = 1.02$$

Since the computations are illustrated in Winer (1971, p. 803-5) we have omitted them here.

SP-1: Control Language

Control Language is typed upper case and comments are in bold and lower case.

```
/PROBLEM
          TITLE IS 'SP-1: WHOLE PLOT ARRANGED IN RCB'.
/INPUT
          VARIABLES ARE 6.
          FORMAT IS FREE.
/VARIABLE NAMES ARE BLOCK, WHOLE, Y1, Y2, Y3, Y4. \Rightarrow input variables
/DESIGN
          GROUPING ARE BLOCK, WHOLE.
                                        ⇒ whole plot classification
```

variables DEPENDENT ARE Y1, Y2, Y3, Y4. ⇒ specifies Y measured for four levels of split plot

LEVEL IS 4.

specifies four levels of split plot NAME IS SUBPLOT. \Longrightarrow split plot classification variable EXCLUDE IS 12. \Longrightarrow model specification for whole plot: assumes full factorial. This statement requests the BLOCK (1) by WHOLE (2) interaction to be pooled with SSE(a)

PRINT. ⇒ requests residuals and predicted values

/END 1 1 3 4 7 6 data organized with all split values for a partic-2 1 6 10 1 11 ular BLOCK by WHOLE combination on the same line 3 1 6 10 4 4 1 2 3 2 1 14 2 2 8 8 2 18 3 2 10 8 9 13

SP-2: Control Language

Note: The whole plot and split plot analysis must be requested in separate runs. The first run gives the correct whole plot analysis but an incorrect split analysis (details follow in the annotations). The second run gives the correct split plot analysis.

Whole Plot Run

```
TITLE IS 'SP-2: SP-1 WITH COVARIATE VARYING WITH SPLIT PLOT'.
/PROBLEM
          VARIABLES ARE 10.
/INPUT
          FORMAT IS FREE.
/VARIABLE NAMES ARE BLOCK, WHOLE, Z1, Z2, Z3, Z4, Y1, Y2, Y3, Y4.
          GROUPING ARE BLOCK, WHOLE.
/DESIGN
          DEPENDENT ARE Y1, Y2, Y3, Y4.
          COVARIATE ARE Z1, Z2, Z3, Z4. \Rightarrow yields an analysis of
                                              covariance
          LEVEL IS 4.
          NAME IS SUBPLOT.
          EXCLUDE IS 12.
          RESIDUAL IS MEAN.
          PRINT.
/END
1 1 1 2 1 2 3 4 7 6
2 1 2 2 0 4 6 10 1 11
3 1 3 5 2 0 6 10 4 4
1 2 2 0 2 4 3 2 1 14
2 2 4 1 3 4 8 8 2 18
 2 3 2 4 7 10 8 9 13
Split Plot Run
           TITLE IS 'SP-2: SP-1 WITH COVARIATE VARYING WITH SPLIT PLOT'.
/PROBLEM
           VARIABLES ARE 5.
/INPUT
           FORMAT IS FREE.
           NAMES ARE BLOCK, WHOLE, SUBPLOT, Z, Y.
/VARIABLE
/DESIGN
           GROUPING ARE BLOCK, WHOLE, SUBPLOT.
           DEPENDENT IS Y.
           COVARIATE IS Z.
           EXCLUDE IS 13,123. \Longrightarrow model specification for split plot:
                                    program assumes full factorial.
           PRINT
/END
                                    statement specifies certain factors
1 1 1 1 3
                                    to be pooled in SSE(b).
1 1 2 2 4
1 1 3 1 7
1 1 4 2 6
           ⇒ for split plot analysis data must be organized in a
                similar arrangement with only one datum per line
3 2 4 7 13
```

SP-3: Control Language

Note: This example unlike the other two covariate examples requires only one run. This is because we are using a CRD and no special design specification is required.

/PROBLEM TITLE IS 'SP-4: WHOLE PLOTS ARRANGED IN CRD WITH CONSTRAINT COVARIATE /INPUT VARIABLES ARE 4. FORMAT IS FREE. NAMES ARE A, Z, Y1, Y2. /VARIABLE /DESIGN GROUPING IS A. DEPENDENT ARE Y1, Y2. ⇒ BMDP requires that two covariables be COVARIATE IS Z, Z. specified here to match the number of LEVEL IS 2. NAME IS B. levels of the split plot. Since Z is PRINT. constant for both levels, its name is /END entered for both. 1 3 10 8 1 5 15 12 1 8 20 14 1 2 12 6 2 1 15 10 2 8 25 20 2 10 20 15 2 2 15 10

References

Dixon, J.W., (1981), <u>BMDP</u> <u>Statistical</u> <u>Software</u>, Berkeley: University of California Press, 726 pp.

Federer, W.T. (1955), <u>Experimental Design</u>, <u>Theory and Application</u>. The Macmillan Co., New York, Chapter 16.

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Searle, S.R., Linear Models, Wiley, N.Y., (1971), 532pp.

Searle, S.R., Hudson, G.F.S., and Federer, W.T. (1985), Annotated Computer Output for Covariance-Text, BU-780-M, Biometrics Unit Mimeo Ser., Cornell University, Ithaca, NY.

Winer, B.J., (1971), <u>Statistical Principles in Experimental Design</u>, McGraw-Hill Book Company, New York: 907pp.

1 PAGE 1 BMDP2V

BMDP2V - ANALYSIS OF VARIANCE AND COVARIANCE WITH REPEATED MEASURES.

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Phone (213) 475-5700 Telex 4992203

Data Organization - all split plot values for a particular BLOCK by WHOLE combination must be in the same observation. See control language

on page 9 for the exact data layout.

Program Version: April 1985

(VM/CMS)
Manual Edition: 1983, 1985 reprint. State NEWS in the PRINT paragraph for a summary of new features.

APRIL 20, 1987 AT 16:43:45

PROCRAM CONTROL INFORMATION

/PROBLEM

/INPUT

TITLE IS 'SP-1: WHOLE PLOT ARRANGED IN RCB'. VARIABLES ARE 6. FORMAT IS FREE. NAMES ARE BLOCK, WHOLE, Y1, Y2, Y3, Y4. GROUPING ARE BLOCK, WHOLE. AVARIABLE ADESIGN

LEVEL IS 4.

NAME IS SUBPLOT. EXCLUDE IS 12. PRINT.

END

Control Language (see page 9 for details)

PROBLEM TITLE IS SP-1: WHOLE PLOT ARRANCED IN RCB

will be referred to by its number below 5 Y3 - Each variable is assigned a number and 4 Y2 3 Y1 2 WHOLE VARIABLES TO BE USED 1 BLOCK 2

INPUT FORMAT IS

MAXIMUM LENGTH DATA RECORD IS 80 CHARACTERS.

DESIGN SPECIFICATIONS - Interpretation of DESIGN paragraph

2 - Variables 1 and 2 (BLOCK & WIOLE) make up the "grouping" or whole plot variables 4 5 6 - Variables 3.4.5 and 6 make up the dependent variable, Y - 4 levels of the split plot variable, SUBPLOT DEPEND = LEVEL = GROUP =

VARIABLE MINIMUM MAXIMUM MISSING CATECORY CATECORY GREATER LESS THAN NO. NAME LIMIT LIMIT CODE CODE NAME THAN OR = TO

→ BMOP assigned names for the levels of the two whole plot variables 1.00000 *1.00000 2.00000 *2.00000 3.00000 *3.00000

1.00000 *1.00000 2.00000 *2.00000

2 WHOLE

1 BLOCK

NOTE -- CATECORY NAMES BECINNING WITH * WERE CENERATED BY THE PROCRAM.

9

GROUP STRUCTURE

	by WIOLE combination for	•				
	→ Frequency of observations in each BLOCK by WIOLE combination for Y1-Y4					
COUNT	† ~	-	-	7	-	-
WHOLE	*1.00000	*2.00000	*1.00000	× 2.00000	*1.00000	*2.00000
BLOCK	¥1.00000					₩3.00000

SUMS OF SQUARES AND CORRELATION MATRIX OF THE ORTHOCONAL COMPONENTS POOLED FOR ERROR 2 IN ANOVA TABLE BELOW

0.20000 1.000 3.00000 0.000 1.000 16.80000 -0.327 -0.945 1.000

SPHERICITY TEST APPLIED TO ORTHOCOUNAL COMPONENTS - TAIL PROBABILITY 0.0

the levels of the split plot are ordered and the investigator is concerned about the assumption of independence and equal variances on the levels of the split plot. However, it will be shown on SP-1 page 5 that the "error 2" or SSE(b) that BMDP computs for this design is incorrect making the above values also incorrect. The above information on the orthogonal components of the split plots are useful when independent and have equal variances (sometimes referred to as symmetry assumption) Tests assumption that the orthogonal components for the split plot, SUBPLOT are

•				% × ₹.			HUYNH FELDT PROB.	= 24.0/8.0	0.0031 0.0428 0.0144	
		-1	6.0000 7.0000 1jk 4.0000 11.0000	7.0000		t) plot)	GREENHOUSE CEISSER PROB.	3.0 = 24	0.0544 0.1719 0.0964	
		MARGINAL	* *		9	e plo iplit	€ 0			
		ì	10.00000 8.00000 9.00000 13.00000	000		(whole	TAIL PROB.	0.0067 0.2500 0.2254	0.0031 0.0428 0.0144	
		*3.0000	10.0 8.0 9.0	10.0000	l fect	= variety effect (whole plot) = fertilizer effect (split plot)	ír.	147.00 3.00 3.00	15.60 4.60 8.40	
			6.00000 10.00000 4.00000 4.00000	6.00000	1 I = block effect	rriety ertilliz	Pring.	4	2 · · ·	15
•		*3.0000	-	9.9	$\frac{1}{p_1 = b!}$	ti II	ARE ARE	76.00000 24.00000 24.00000 8.00000	52,00000 15,3333 28,0000 3,3333	
			8.00000 8.00000 2.00000 18.00000	9.00000	•	- 3	MEAN SQUARE	22	52.0 15.3 28.0 3.3	
		*2.0000		9.6	1		S OF	MSE(a)		
	=		6.00000 10.00000 1.00000 11.00000	7.00000	8	Y	DECREES OF FREEDOM	- 2 - 2	<i></i>	
	1-ST DEPENDENT VARIABLE	*2.0000 *1.0000		7.	D IN R	•	SUM OF SQUARES	76,00000 48,00000 24,00000 16,00000	156.00000 92.00000 84.00000 20.00000	
	NDENT		3.00000 2.00000 1.00000	5.00000	RRANGE	73	SUM OF SQUARE	=		
	т рере	*1.00000 *2.00000	2 - 4	ů.	ntot /	st 72	!	(1)2 =	→ see note below	
			8888	5.00000	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	FOR 1-ST		SSM=N ⁷ =24(7) ² μ) μ, ρ.τ)		
	MEANS FOR	*1.00000	3.0000 4.0000 7.0000 6.0000	1.1 = 5.	1 SP-1:) 원		SSM= R(ρ μ) R(τ μ) R(δ μ.ρ.	SUBPLOT R(α μ) SB SW R(ατ μ,α.τ) ERROR incorrect	
	CEIT ME	= subs	LOT = 2 2 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	NAL Y	BMDP2V	OF VARIANCE	SOURCE		SUBPLOT SB SW R(ar	
,	J	= BLOCK = WHOLE		MARGINAL	COUNT	ANALYSIS OF VARIANG	306	MEAN BLOCK WHOLE ERROR	SUB SB SB ERRI	
		c 	71 72 73			ANAL		-	8	

N

HUYNH-FELDT

SP-1, page 5 The "2 error" or SSE(b) reported here is incorrect. This means that Greenhouse-Ceisser & Huynh-Feldt are adjusted p-values to be used when the symmetry assumptions on the split plot are not met (see sphericity test on SP-1 page 3). However, these values are incorrect for this design because BMDP has computed the SSE(b) incorrectly. See the note below.

The "2 error" or SSE(b) reported here is incorrect. This means the F statistics and associated tail probabilities for the split plot portion of the analysis are also incorrect. To obtain the correct SSE(b) it is necessary to pool the SS's labelled SB(SUBPLOTWBLOCK) with the SS's labelled "Z error". I.E. 92+20 = 112. The F statistics for SUBPLOT(F) and SW(SUBPLOTWHOLE) need to be recalculated using this corrected SSE(b).

> = 5.57 112/12 FSUBPLOT = 156/3

= 3.0 112/12 FSUBPLOT*WHOLE = 84/3

OF SQUARES

CORRESPONDING RESIDUALS

R1, R2, R3, R4 BNDP2V SP-1: WHOLE PLOT ARRANGED IN RCB

bage 6	
SP-1,	

ဇ္									
	-1.00000	0.0000	1.00000	1.00000	0.00000	-1.00000		ູ້	•
S	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000		0 = 1.0 = R	
Z.	$2.00000 \text{ RO}_1 = 1.00000$	0.0000	-1.00000	-1.00000	0.00000	1.00000		$\vec{Y}_{11} = \hat{Y}_{11} = 5.0 - 4.0 = 1.0 = \text{RO}_1$	
8	RO1	ı						, , ,	
	2.00000	3.50000	-2.50000	8.00000	9.50000	3.50000		Υ <u>.</u>	:
P4	0	0	0	0	0	0			
	0.0000	-5.50000	-0.50000	-2.00000	-7.50000	-2.50000			
F3	8	8	8	8	8	8			
	0.00000	3.00000	3.00000	-4.00000	-1.00000	-1.00000			
P2	-2.00000	-1.00000	0.50000	-2.0000	1.0000	0.0000	RELATIVE	ERROR	0.00000
P1 R4	= 4.00000	2.00000	7.0000 7.0000	6.0000	00000	9.0000	RECOMPUTED	FROM RESIDUALS	16.00000
8.8	Ŷ.						REC	FROM	91 02
WHOLE	*1.00000 *1.00000 $\hat{Y}_{11*} = 4.0$	*2.00000 *1.00000	*3.00000 *1.00000	*1.00000 #2.00000	*2.00000 *2.00000	*3.00000 *2.00000	SUM OF	SQUARES	16.00000
BLOCK	*1.0000	*2.0000C	¥3.0000	*1.00000	¥2.0000	¥3.0000€		8	20.
CASE	-	8	က	4	2	9	ERROR	TERM	7

CPU TIME USED 0.183 SECONDS

PO & RO are whole plot predicted values and residuals, respectively.

PI-P4 and RI-R4 are supposed to be split plot predicted values and residuals respectively but are computed from an incorrect value for SSE(b) (see previous page) and should therefore be ignored.

SP-2. SP-1 data with a covariate added and varying from split plot to split plot, first run.

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Phone (213) 475-5700 BMDP Statistical Software, Inc. 1964 Westwood Blvd. Suite 202 Los Angeles, California 90025

layout.

Data Organization - all split plot values for Z and Y or a particular BLOCK by WHOLE combination must be in the same observation. See control language on page 10 for exact data

Program Version: April 1985

Manual Edition: 1983, 1985 reprint. State NEWS in the PRINT (VIVORS)

paragraph for a summary of new features.

APRIL 20, 1987 AT 16:44:22

PROCRAM CONTROL INFORMATION

TITLE IS 'SP-2: SP-1 WITH COVARIATE VARYING WITH SPLIT PLOT'. /PROBLEM

/INPUT

VARIABLES ARE 10. FORMAT IS FREE. NAMES ARE BLOCK, WHOLE, Z1, Z2, Z3, Z4, Y1, Y2, Y3, Y4. GROUPING ARE BLOCK, WHOLE. VARIABLE

Control Language (see page 10 for details)

DEPENDENT ARE Y1, Y2, Y3, Y4. COVARIATE ARE Z1, Z2, Z3, Z4. DESIGN

LEVEL 1S 4.

NAME IS SUBPLOT.

EXCLUDE 1S 12. RESIDUAL IS MEAN. PRINT

18

Sand Parties

Contract Contract Authority

" " Secretary | 1466/6/60" Established | Contractory

PROBLEM TITLE 1S SP-2: SP-1 WITH COVARIATE VARYING WITH SPLIT PLOT

10	0	10	TO END		NEITHER	MISSING	32362
NUMBER OF VARIABLES TO READ IN	NUMBER OF VARIABLES ADDED BY TRANSFORMATIONS.	TOTAL NUMBER OF VARIABLES	NUMBER OF CASES TO READ IN TO END	CASE LABELING VARIABLES	MISSING VALUES CHECKED BEFORE OR AFTER TRANS	BLANKS ARE.	NUMBER OF WORDS OF DYNAMIC STORAGE
NUMBER OF VAR	NUMBER OF VAR	TOTAL NUMBER	NUMBER OF CAS	CASE LABELING	MISSING VALUE	BLANKS ARE.	NUMBER OF WOR

2 WHOLE 7 Y1 VARIABIES TO BE USED 1 BLOCK 6 24

INPUT FORMAT IS

FREE

5 Z3 10 Y4

4 Z2 9 Y3

80 CHARACTERS. MAXIMUM LENCTH DATA RECORD IS

DESIGN SPECIFICATIONS

9 GROUP =
DEPEND =
COVAR =
LEVEL = INTERVAL RANGE GREATER LESS THAN THAN OR = TO MISSING CATEGORY CATEGORY CODE. ONDE. NAME. MAXIMUM LIMIT MINIMUM VARIABLE NO. NAME

1 BLOCK

2 WHOLE

1.00000 *1.00000 2.00000 *2.00000 3.00000 *3.00000

1.00000 *1.00000 2.00000 *2.00000

6

NOTE -- CATEXORY NAMES BEGINNING WITH * WERE GENERATED BY THE PROGRAM.

GROUP STRUCTURE

COUNT	_	-	-	-	-	_
WHOLE	*1.00000	*2.00000	*1.00000	*5.00000	*1.00000	*2 00000
BLOCK	*1.00000	*1.00000	*2.00000	*2 .00000	₩3.00000	*3 00000

SUMS OF SQUARES AND CORRELATION MATRIX OF THE ORTHOCONAL COMPONENTS POOLED FOR ERROR 2 IN ANOVA TABLE BELOW

		1.00
	000.1	-0.979
1.000	-0.907	0.802
0.01156	3.07111	16.65067

INSUFFICIENT DECREES OF FREEDOM FOR SYMMETRY TEST

Like in SP-1, these values on the orthogonal components are incorrect because they are based on "Error 2" or SSE(b) which is computed incorrectly. See SP-1 page 3 and 5 for details.

CELL MEANS FOR 1-ST COVARIATE

	Z
	2.50000 2.00000 2.00000 3.50000
MARGINAL	2 1.3k
#3.00000 #2.00000	3.00000 2.00000 4.00000 7.00000
*3.00000	3.00000 5.00000 2.00000 0.00000
*2.00000 *2.00000	4.00000 1.00000 3.00000 4.00000
*2.00000 *1.00000	2.00000 2.00000 0.00000 4.00000
*1.00000	2.00000 0.00000 2.00000 4.00000
*1.00000	1.0000 2.0000 1.0000 2.0000
SURP	LOJ - 62 & 4.
j = BLOCK i = WHOLE	2 222

•					: :			
$2.50000 = \vec{Z}_{\bullet\bullet}$	9	MADONA	TANK TIVET	6.00000	Y 7.00000 ijk 4.00000	11.00000]	$7.00000 = \overline{\mathbf{Y}}$	9
4.00000			*3.00000 *2.00000	10.00000	8.00000	13.0000]	10.00000	-
2.50000	1		*3.00000	6.00000	10.00000	4.00000	6.00000	-
3.00000	-		*2.00000	8.00000	8.00000	18.00000	9.0000	-
2.0000	-	VARIABLE	*2.00000	6.00000	10.00000	11.00000	7.00000	-
2.00000	-	ST DEPENDENT	*1.00000	3.0000	2.00000	14.00000	5.00000	1
.j•= 1.50000	1	CELL MEANS FOR 1-ST DEPENDENT VARIABLE	1.00000	= lk 3.0000	4.00000	00000	1j•≈ 5.00000	
MARCINAL Z	COUNT	CEIT	J = BLOCK = 1 = WHOLE =	SUBP LOT = 1	3.8	4	MARGINAL Ÿ	COUNT
				Y1	Y2 Y3	7		

BMDP2V SP-2: SP-1 WITH COVARIATE VARYING WITH SPLIT PLOT

PENDE	ANALYSIS OF VARIANCE FOR DEPENDENT VARIABLE - YI SOURCE BLOCK R(p µ, T, p 1, whole R(T µ, p, p 1, whole R(T µ, p, p 1, p 1, p 2, p 3, p 3, p 4, p 4, p 4, p 4, p 4, p 4	1-ST γ2 α,ατ) α,ατ) ρ.τ.α.ατ)	Y3 SUM OF SQUARES 15.60000 3.42857 16.00000 0.00000 77.91667 50.23859 0.23859	Y4 DECREES OF FREEDOM 1 1 1 3 6 6 6	HEAN F SQUARE 7.90000*********************************	8 89 4.24 0.07	TA1L PROB. 0.0000 0.0000 0.0000 0.0190 0.0768 0.8053	GREENHOUSE GEISSER PROB. 0.1152 0.2624 0.1992	HUYNH FELDT PROB. 0.0190 0.1063	RECRESSION COEFFICIENTS $4.00000 = \hat{\boldsymbol{\beta}}_1$ 0.13333
	ERROR	•	19,73333	5	3.94667					
	ERROR			n	ionte c					
ERROR		EPSILON FACTORS FOR		DECREES OF FREEDOM ADJUSTMENT	ADJUSTMENT					
		GREENHOUSE-GEISSER		HUYNII-FELDT						

FOOLED RECRESSION COEFFICIENTS → The BMOP manual states that this estimate is "obtained from the weighted pooled cross-product matrix"

... and is used to compute adjusted cells means". This is probably of no interest to the experimenter.

1-ST COVARIATE

4.00000

The "2 error" or SSE(b) reported here is incorrect. This causes the SS's for the covariate in the above analysis to be incorrect also, thereby causing the SS's for SUBPLOT and SUBPLOT=WHOLE labelled (SW) to be adjusted incorrectly. The reason "2 error" or SSE(b) is wrong is because the SS's for SUBPLOT=BLOCK (labelled SB) should be pooled with "2 error". Another call to BMDP is required to get the correct split plot portion of the analysis and this begins on SP-2 page 8.

ERROR SUM OF SQUARES

CORRESPONDING RESIDUALS

 \vec{Y}_{11} , $-\hat{Y}_{11}$, = 5.0 - 5.0 = 0.0 = $\mathbf{R0}_1$ 1 = SSE(a) RO 2 ≠ SSE(b) R1, R2, R3, R4 4 BMDP2V SP-2: SP-1 WITH COVARIATE VARYING WITH SPLIT PLOT 1 PACE

22	-0.96667	0.06667	0.90000	0.96667	-0.06667	-0.90000	
R1	0.03333	0.06667	-0.10000	-0.03333	-0.06667	0.10000	
RO	$Ro_1 = 0.00000$	0.00000	0.0000	0.00000	0.00000	0.0000	
P4	2.03333 RO	3.70000	-2.73333	7.96667	9.30000	3.73333	
P3	0.03333	-5.56667	-0.46667	-2.03333	-7.43333	-2.53333	
22	-0.03333	2.93333	3.10000	-3.96667	-0.93333	-1.10000	
P1 R4	-2.03333	-1.03333	0.30000	0.7333	0.93333	-0.30000 -0.10000 -0.73333	RESIDUALS ERROR . 00000HHHHHHHHHHHHHHHHHHHHHHHHHHHHHHHH
S 55	$\hat{\mathbf{r}}_{11}$ = 5.0000		6.0000	-1.53333	-1.96667 9.00000	0.43333 10.00000 1.53333	RECOMPUTED FROM RESIDUALS 0.00000000000000000000000000000000000
BLOCK WHOLE	*1.00000 *1.00000 Ŷ11*	*2.00000 *1.00000	#3.00000 #1.00000	*1.00000 *2.00000	#2.00000 #2.00000	*3.00000 *2.00000	SUM OF SQUARES 0.00000 19.73333
CASE	-	8	m	₹	ທ	9	ERROR TERM 1

ADJUSTED CELL MEANS ARE NOT COMPUTED WHEN THE INCLUDE OPTION IS USED. → BMDP cannot compute adjusted means for anything other than straight factorials.

0.213 SECONDS CPU TIME USED PO and RO are whole plot predicted values and residuals, respectively. PI-P4 and RI-R4 are supposed to be split plot predicted values and residuals but are computed from an incorrect value for SSE(b) (see previous page) and should therefore be ignored (correct values are computed in the run that follows).

SP-2 Split Plot, second run

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measurement per observation. See control language on page 10 for exact data layout. Rata Organization: Data arranged with only one Z and Y

Program Version: April 1985 (VM/CMS) Manual Edition: 1983, 1985 reprint. State NEWS in the PRINT paragraph for a summary of new features.

APRIL 10, 1987 AT 15:36:42

PROCRAM CONTROL INFORMATION

VARIABLES ARE 5.
VARIABLES ARE 5.
FORMAT IS FREE.
NAMES ARE BLOCK, WHOLE, SUBPLOT. Z. Y.
GROUPING ARE BLOCK, WHOLE, SUBPLOT.
DEPENDENT IS Y.
COVARIATE IS Z.
EXCLUDE IS 13,123.
PRINT. /PROBLEM

/INPUT

/VARIABLE /DESIGN

ES

Control Language (see page 10 for details)

PROBLEM TITLE IS SP-2: SP-1 WITH COVARIATE VARYING WITH SPLIT PLOT

2	0	5	TO END		NEITHER
•	٠	•	•	٠	•
NUMBER OF VARIABLES TO READ IN	NUMBER OF VARIABLES ADDED BY TRANSFORMATIONS.	TOTAL NUMBER OF VARIABLES	NUMBER OF CASES TO READ IN TO END	CASE LABELING VARIABLES	MISSING VALUES CHECKED BEFORE OR AFTER TRANS NEITHER

INPUT FORMAT IS FREE

MAXIMUM LENCTH DATA RECORD IS 80 CHARACTERS.

DESIGN SPECIFICATIONS

 $\begin{array}{rcl} \text{GROUP} &=& 1 & 2 \\ \text{DEPEND} &=& 5 \\ \text{COVAR} &=& 4 \end{array}$

					INTERV	INTERVAL KANGE	
VARIABLE	MINIMUM	MAXIMUM	CATECORY	MISSING CATECORY CATECORY	GREATER	GREATER LESS THAN	
NO. NAME	LIMIT	LIMIT	CODE	NAME	THAN	OR = TO	
1 BLOCK							
			1.00000	.00000 ×1.00000			
			2.00000	2.00000 ★2.00000			
			3.00000	3.00000 ★3.00000			
2 WHOLE							
			1.00000	1.00000 ★1.00000			
			2.00000	2.00000 *2.00000			
3 SUBPLOT							
			1.00000	1.00000 *1.00000			
			2.00000	2.00000 *2.00000			
			3.00000	3.00000 ★3.00000			
			4.00000	4.00000 *4.00000			

NOTE--CATECORY NAMES BEGINNING WITH * WERE GENERATED BY THE PROCRAM.

NUMBER OF CASES READ.

24

56

PLOT
SPLIT
ITH S
VARYING N
COVARIATE
WITH
SP-1
SP-2:
BMDP2V

	BMDP2	BMDP2V SP-2: SP-1 WITH COVARIATE VARYING WITH SPLIT PLOT	OVARIATE VAR	YING WITH SPL	IT PLOT	م = لو الم = الم	$p_j = \text{block effect}$ $\alpha_i = \text{subplot effect}$	$p_j = \text{block effect}$ $\alpha_i = \text{subplot effect (split plot)}$	$r_1 = whole plot effect$ $\beta_0 = slope for split plot$
ANALY DEPEN	ANALYSIS OF VARIANCE F DEPENDENT VARIABLE - Y	ANALYSIS OF VARIANCE FOR 1-ST DEPENDENT VARIABLE - Y				×			
	SOURCE		SUM OF SQUARES	DECREES OF FREEDOM	MEAN SQUARE	ĹĽ.	TAIL PROB.	RECRESSION COEFFICIENTS	
	BLOCK	I CNORE*	20.20862		10.10431	1.14	0.3551		
	WHOLE	ICNORE* $R(\alpha \mu,\rho,\tau,\alpha\tau,\beta_2)$	6.10385 84.24310	3 H	6.10385 28.08103	0.69	0.4244 0.0678		
	BW	ICNORE* $R(\alpha\tau \mu,\rho,\tau,\alpha,\beta_2)$	9.45000	3.2	. 4.72500 12.49146	0.53	0.6014		
	2	$R(\beta_2 \mu,\rho,\tau,\alpha,\alpha\tau)$	14.45000	-	14.45000	1.63	0.2281	$0.85000 = \hat{\beta}_{2}$	
-	ERROR	SSE(b)	97.55000	11	8.86818			3	

*These whole plot effects were estimated correctly in the 1st call to BMDP on SP-2 page 6 and should be ignored here.

ACCEMBANANCE SECRETARIA SOCIAL

BMDP2V SP-2: SP-1 WITH COVARIATE VARYING WITH SPLIT PLOT

residuals	E: If the correct error SSE(b) sums of squares are to be obtained, we need to use the line "EXCLUDE IS 13,123." However, this does not allow the means to be adjusted for covariance. If the above statement is deleted from the program, adjusted means will be obtained but they are incorrect because SSE(b) is computed incorrectly.	
RESIDUAL = split plot residuals	3.0 - 3.575 = NOTE:	
RESIDUAL =	-0.57500 = 3.0 - 3.575 = -0.575 -2.57500 3.57500 -0.42500 1.85000 -1.85000 0.72500 -0.42500 0.72500 -0.87500 1.00000 1.00000 2.00000 1.85000 1.85000 1.85000 -3.85000 1.85000 -4.85000 -4.85000 -2.85000 -4.85000	. 8
PREDICTD	= 3.575 6.575 6.000 6.000 6.000 6.000 6.000 6.000 7.0000 7.000 7.000 7.000 7.000 7.000 7.000 7.000 7.000 7.0000 7.000 7.000 7.000 7.000 7.000 7.000 7.000 7.000 7.00000 7.0000 7.0000 7.0000 7.0000 7.0000 7.0000 7.0000 7.0000 7.0000 7.0000 7.	0.0000 0.0000
Lor	Y ₁₁₁	97.55000
SUBPLOT	#1.00000 #1.00000 #1.00000 #3.00000 #1.00000 #3.00000 #1.00000 #3.00000 #1.00000 #3.00000 #1.00000 #3.00000 #1.00000 #3.00000 #1.00000 #3.00000 #1.00000 #3.00000 #2.00000 #3.00000 #2.00000 #3.00000 #2.00000 #3.00000 #2.00000 #3.00000 #2.00000 #3.00000 #2.00000 #3.00000 #2.00000 #3.00000 #2.00000 #3.00000 #2.00000 #3.00000	6
WHOLE	#1.00000 #1.00000 #1.00000 #2.00000 #1.00000 #1.00000 #3.00000 #2.00000 #1.00000 #3.00000 #2.00000 #1.00000 #3.00000 #3.00000 #1.00000 #3.00000 #3.00000 #1.00000 #3.00000 #3.00000 #1.00000 #3.00000 #3.00000 #1.00000 #3.00000 #3.00000 #1.00000 #3.00000	97.55000
BLOCK	1. 10000 1. 1. 1. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2. 2.	1 S
CASE	11 12 13 15 15 16 18 18 18 18 18 18 18 18 18 18 18 18 18	1 FK

ADJUSTED CELL MEANS ARE NOT COMPUTED WHEN THE INCLUDE OPTION IS USED.

CPU TIME USED 0.216 SECONDS

ENTERNA PORT

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SP-3. Whole Plots Arranged in CRD With Constant Covariate Within Whole Plot

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Phone (213) 475-5700 Telex 4992203

Los Angeles, California 90025

Program Version: April 1985

Manual Edition: 1983, 1985 reprint. State NEWS in the PRINT (VICORS)

paragraph for a summary of new features.

MAY 1, 1987 AT 14:21:52

PROCRAM CONTROL INFORMATION

/PROBLEM TITLE IS 'SP-3: WHOLE PLOTS ARRANGED IN CRD WITH

CONSTANT COVARIATE:

/ INPUT VARIABLES ARE 4.

FORMAT IS FREE.

//VARIABLE NAMES ARE A, Z, Y1, Y2.

//DESIGN GROUPING IS A.

DEPENDENT ARE Y1, Y2.

COVARIATE IS Z, Z.

LEVEL IS 2.

Bata Organization - all split plot values for a particular SUBJECT by A combination must be in the same observation. See Control Language on Page 11 for the exact data layout

Control Language (see page 11 for details)

PROBLEM TITLE IS SP-3: WHOLE PLOTS ARRANGED IN CRD WITH CONSTANT COVARIATE

404	TO END	NEITHER MISSING	32362
		• •	•
NUMBER OF VARIABLES TO READ IN. NUMBER OF VARIABLES ADDED BY TRANSFORMATIONS. TOTAL MINNER OF VARIABLES	NUMBER OF CASES TO READ IN. CASE I PARTABLES	MISSING VALUES CHECKED BEFORE OR AFTER TRANS. RI ANKS ARE	NUMBER OF WORDS OF DYNAMIC STORAGE.

VARIABLES TO BE USED

1 A 2 Z 3 Y1

4 Y2

7 Z V

INPUT FORMAT IS FREE MAXIMUM LENGTH DATA RECORD IS 80 CHARACTERS.

DESIGN SPECIFICATIONS

VARIABLE MINIMUM MAXIMUM MISSING CATECORY CATECORY GREATER LESS THAN NO. NAME LIMIT LIMIT CODE CODE NAME THAN OR = TO

1.00000 *1.00000 2.00000

NOTE--CATECORY NAMES BEGINNING WITH * WERE GENERATED BY THE PROGRAM.

NUMBER OF CASES READ.

8

0000 10000

100 m

CONTRACTOR CONTRACTOR

CROUP STRUCTURE

A COUNT #1.00000 4 #2.00000 4 CELL MEANS FOR 1-ST COVARIATE

MARGINAL A = *1.00000 *2.00000 B Z 1 4.50000 5.25000 4.87500 Z 2 4.50000 5.25000 4.87500 MARCINAL 4.50000 5.25000 4.87500 COUNT 4 4 8

STANDARD DEVIATIONS FOR 1-ST COVARIATE

A = *1.00000 *2.00000

1 2.64575 4.42531 2 2.64575 4.42531

2

CELL MEANS FOR 1-ST DEPENDENT VARIABLE

MARGINAL		
	¥2.00000	
	¥1.00000	
	11	20
	<	

16.50000 14.18750 ထ 18.75000 16.25000 14.25000 12.12500 MARGINAL SOUNT TWO 72

STANDARD DEVIATIONS FOR 1-ST DEPENDENT VARIABLE

*2.00000 ¥1.00000 11

4.78714 4.34933 Y1

 $\beta_1 = Z$ slope for whole plot $\tau_i = \Lambda$ effect (whole plot) BADP2V SP-3: WHOLE PLOTS ARRANGED IN CRD WITH CONSTANT COVARIATE

α_k = B effect (split plot)

1-51 ANALYSIS OF VARIANCE FOR DEPENDENT VARIABLE - Y1

RECRESSION COEFFICIENTS TAIL PROB. MEAN DECREES OF SUM OF SQUARES

 $1.02194 = \hat{\beta}_1$ 0.0001 0.0142 0.1151 3.63 13.59 80.53 0.53 166.57680 12.25964 85.56250 0.56250 1.06250 44.49160 SQUARE FREEDOM 166.57680 61.29820 85.56250 0.56250 6.37500 44.49160 $A(whole plot)R(\tau|\mu.\beta_1.\alpha.\alpha\tau)$ B(split plot)R(α | $\mu, \tau, \beta_1, \alpha\tau$)
BA
R($\alpha\tau$ | $\mu, \tau, \beta_1, \alpha$)
ERROR
SSE(b) 1-ST COVAR $R(\beta_1 | \mu, \tau, \alpha, \alpha \tau)$ ERROR SSE(a) SOURCE

CORRESPONDING RESIDUALS ERROR SUM OF SQUARES

8

R0 R1. R2

STATE OF THE PROPERTY OF THE P

1

\$

BMDP2V SP-3: WHOLE PLOTS ARRANGED IN CRD WITH CONSTANT COVARIATE

6 = -1.6		0	0	0	0	0	0	0	0		The means \vec{Y}_{i-k} are adjusted only for the whole
$= \overline{Y}_{11}, - \widehat{Y}_{11}, = 9.0 - 10.6 = -1.6$	SZ	1.12500	0.62500	-0.8750	-0.8750	0.000	0.00000	0.0000	0.000		The
	R1	-1.12500	-0.62500	0.87500	0.87500	0.0000	0.0000	0.0000	0.00000		
	RO	-1.59208	0.86403	1.29820	-0.57014	0.59326	3.43965	-3.60423	-0.42868		
	22	-2.12500	-2.12500	-2.12500	-2.12500	-2.50000	-2.50000	-2.50000	-2.50000	RELATIVE ERROR 0.00000	0.0000
	P1	2.12500	2.12500	2.12500	2.12500	2.50000	2.50000	2.50000	2.50000	PUTED SIDUALS 3820	6.37500
	2	$\hat{\mathbf{Y}}_{11} = 10.59208$	12.63597	15.70180	9.57014	11.90674	19.06033	21.10422	12.92868	RECOMPUT FROM RESID 0 61.2982	
	⋖	*1.00000 Î	*1.00000	*1.00000	*1.00000	*2.00000	*2.0000	*2.00000	* 2.00000	SUM OF SQUARES 61.29820	6.37500
	CASE	-	8	က	4	S	9	7	∞	ERROR TERM 1	8

ADJUSTED CELL MEANS FOR 1-ST DEPENDENT VARIABLE

plot covariate because the covariate is constant

for all split plots within one whole plot. The

PO and RO are whole plot predicted values and residuals, respectively. PI-P2 and RI-R2 are split plot predicted values and residuals.

$$Y_{i,jk} = P0 + R0 + Pj + Rj$$

e.g.
 $Y_{i,i,j} = 10.59208 - 1.59208 + 2.125 - 1.125 = 10.00$

END DATE FILMED DEC. 1987